



**FRSGlobal**

# **SOLVENCY RISK CAPITAL MODELS FOR THE INSURANCE BUSINESS**

**March, 2010**

# Agenda

## ● Swiss Solvency Test (SST)

## ● The cost-of-capital (CoC) approach

## ● The prospective liability approach

## ● Solvency II and SST applications

- Non-Life Underwriting Risk
- Life Underwriting Risk
- Market Risk

## ● References / Discussion / Q&A

# SST (1) economic balance sheet / fair value of liabilities

## Assets



## Liabilities



Free Capital  
Economic Capital (EC)  
Risk Margin (RM or MvM)  
Best estimate of Liabilities

- **Fair value = Best estimate + Risk margin (MvM)**
- **Two methods** for Risk Margin (MvM) evaluation:
  - **CoC approach**
  - **Prospective liability approach / quantile approach**
- **SST summary**  
**Kaufmann, Wyler(2005)**

Risk Bearing Capital = Available Capital + Risk Margin  
= Market value of Assets - Best estimate of Liabilities  
Market value of Liabilities = Best estimate + Risk Margin  
Available Capital = Market value of Assets - Market value of Liabilities  
Target Capital = Economic Capital + Risk Margin

- **Doff(2007)**, Chapter 6, pp. 103-106
- **Hürlimann(2009a)**, pp.447-450

# SST (2) Target capital TVaR(99%) for Life & Non-Life

SOLVENCY CAPITAL REQUIREMENT RESULTS				Values in Mio. ....
	Standard Deviation	Value-at-Risk	Expected Shortfall	
<b>Aggregation without Scenarios</b>				
Insurance Risk	x	x	x	
Life	x	x	x	
Non-Life	x	x	x	
Market Risk	x	x	x	
Insurance & Market Risk	x	x	x	
Diversification Benefit		x	x	
<b>Aggregation with Scenarios</b>				
Insurance & Market Risk		x	x	
<b>Aggregation with other Risks</b>				
Credit Risk (Basle II)	x	x		
Operational Risk	x	x		
Total Risk	x	x		
Total Diversification benefit	x	x		
<b>Risk Margin (Market value Margin)</b>				
<b>Target Capital</b>				
<b>Risk Bearing Capital</b>				
<b>Ratio of Target Capital to Risk Bearing Capital</b>				

# SST (3) Public Disclosure TVaR(99%) (SwissRe 2006-08)

ONE-YEAR 99% TVaR (EXPECTED SHORTFALL)		billion	CHF	
Group Level Aggregation		2008	2007	2006
Property & Casualty		7.9	8.6	10.0
Life & Health		5.2	5.9	6.5
Financial Market		8.0	7.7	7.7
Credit		3.0	2.8	2.1
Funding & Liquidity				0.3
Total Diversification Effect		9.1	8.5	8.9
Swiss Re Group		15.0	16.5	17.7

# CoC approach (1) stochastic insurance model



## Multi-period discrete time stochastic model of insurance

$A(t)$	: <i>assets</i> at time $t$
$L(t)$	: <i>actuarial liabilities</i> at time $t$
$C(t) = A(t) - L(t)$	: <i>risk-bearing capital</i> (RBC) at time $t$ (actuarial surplus)
$P(t-1)$	: <i>loaded premium</i> paid at time $t-1$ (fully invested)
$X(t)$	: <i>insurance costs</i> paid at time $t$ (insurance benefits, expenses and bonus payments for period $(t-1,t]$ )
$\pi(t-1)$	: <i>pure premium</i> at time $t-1$ (cover insurance costs)
$\Theta(t-1) = P(t-1) - \pi(t-1)$	: <i>premium loading</i> at time $t-1$
$R(t)$	: accumulated <i>rate of return</i> on investment for period $(t-1,t]$
$v=1/r$	: <i>risk-free discount rate</i> ( $r$ is risk-free accumulated rate)

Equation of dynamic evolution of the random assets over the time horizon  $[0,T]$ :

$$A(t) = (A(t-1) + P(t-1)) \cdot R(t) - X(t), \quad t=1, \dots, T$$

# CoC approach (2) Economic and Target Capital



## ⌚ Discounted shortfall RBC and its time period change

$$SC(t) = v^t \cdot (L(t) - A(t)), \quad \Delta SC(t) = SC(t) - SC(t-1), \quad t=1, \dots, T$$

## ⌚ Economic capital (EC)

$$EC = R[\Delta SC(1)], \quad R[\cdot] \text{ risk measure (e.g. VaR, TVaR)}$$

## ⌚ Risk Margin (RM) / Market value Margin (MvM)

$$RM = i_{CoC} \cdot (R[\Delta SC(2)] + R[\Delta SC(3)] + \dots + R[\Delta SC(T)])$$

$i_{CoC}$  : *cost-of-capital rate* (spread between borrowing and reinvesting)

## ⌚ Target Capital (TC)

$$TC = EC + RM$$

# CoC approach (3) VaR & TVaR (SST) target capital

## ● VaR target capital

$$TC_{\alpha, \text{VaR}} = A(0) - L(0) + \text{VaR}_{\alpha} [ v \cdot (L(1) - A(1)) ]$$

$$+ i_{\text{CoC}} \cdot \sum_{(t=2, \dots T)} \text{VaR}_{\alpha} [ v^t \cdot (L(t) - r \cdot L(t-1)) - v^t \cdot (A(t) - r \cdot A(t-1)) ]$$

## ● TVaR target capital = SST target capital (**FOPI(2004/06)**)

$$TC_{\alpha, \text{TVaR}} = A(0) - L(0) + \text{TVaR}_{\alpha} [ v \cdot (L(1) - A(1)) ]$$

$$+ i_{\text{CoC}} \cdot \sum_{(t=2, \dots T)} \text{TVaR}_{\alpha} [ v^t \cdot (L(t) - r \cdot L(t-1)) - v^t \cdot (A(t) - r \cdot A(t-1)) ]$$

$\text{TVaR}_{\alpha}[ X ] = E [ X | X > \text{VaR}_{\alpha}[X] ]$  (*tail value-at-risk* for continuous distribution functions)

# Prospective liability approach (1) risk-free asset values

## ● Prospective insurance liability and premium loading

$CF(t) = v \cdot X(t+1) - \pi(t)$  : *insurance cash-flow* at time  $t$  period  $(t, t+1]$ ,  $t=0, \dots, T-1$

$L(t) = \sum_{j=0, \dots, T-t-1} v^j \cdot CF(t+j)$  : *prospective insurance liability* at time  $t=0, \dots, T-1$

$\Theta(t) = \sum_{j=0, \dots, T-t-1} v^j \cdot \Theta(t+j)$  : *prospective premium loading* at time  $t=0, \dots, T-1$

## ● Risk-free asset valuation

The equation of dynamic evolution of the assets valued at the risk-free rate yields

$A(t+\tau) = ( A(t+\tau-1) + P(t+\tau-1) ) \cdot r - X(t+\tau) = ( A(t+\tau-1) - CF(t+\tau-1) + \Theta(t+\tau-1) ) \cdot r, \quad \tau=1, \dots, T-t,$

=> relationship  **$A(t+\tau) + \Theta(t+\tau) - L(t+\tau) = r^\tau \cdot ( A(t) + \Theta(t) - L(t) ), \quad \tau=1, \dots, T-t-1$**

# Prospective liability approach (2) VaR solvency criterion

## Liability VaR solvency criterion

Assets and premium loadings should exceed liabilities with high probability at each future time until ultimate liabilities vanish (run-off situation):

$$P( A(t+\tau) + \Theta(t+\tau) \geq L(t+\tau), \tau=1, \dots, T-t-1 ) \geq 1 - \epsilon \quad (\text{QIS4(2008)}: \text{probability of loss } \epsilon=0.5\%)$$

$$<=> \text{ (from preceding relationship)} \quad P( A(t) + \Theta(t) \geq L(t) ) \geq 1 - \epsilon, \quad t=0, \dots, T-1$$

$A^*(t) = \text{VaR}_\alpha[L(t)] - \Theta(t)$ ,  $\alpha=1-\epsilon$ , minimum solution of probabilistic inequality

Let  $V(t) = E[L(t)]$  be the *actuarial reserves* (best estimate of insurance liabilities)

$TC^*_{\alpha, \text{VaR}}(t) = \text{VaR}_\alpha[L(t)] - V(t)$  : *insurance risk VaR target capital*  
(available capital to meet the insurance risk)

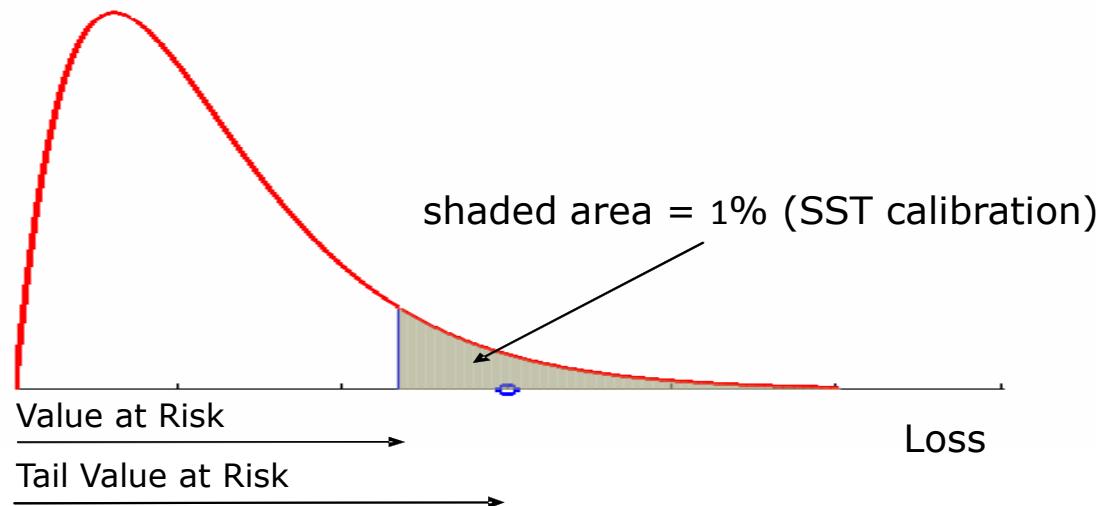
# Prospective liability approach (3) TVaR solvency criterion

## Liability TVaR solvency criterion

The tail value-at-risk measure is *coherent* and has been extensively studied and applied to assess the *solvency risk for insurance liabilities* (e.g. **Hürlimann(2001/02/03)**):

$$TC^*_{\alpha, TVaR}(t) = TVaR_{\alpha}[L(t)] - V(t): \text{insurance risk TVaR target capital}$$

## Graphical representation of VaR and TVaR risk measures



# Solvency II and SST applications



## ● Non-Life Underwriting Risk

- liability VaR criterion vs. standard QIS4 SCR formula / Solvency II vs. SST
- **Gisler(2009), Hürlimann(2010a)**

## ● Life Underwriting Risk

- application of the liability VaR & TVaR criteria / Solvency II vs. Partial Internal Model
- **Hürlimann(2010b)**

## ● Market Risk

- application of the cost-of-capital VaR & SST target capital formulas
- **Hürlimann(2009a)** + important improvements (this presentation)

# Market Risk (1) random assets & market risk model

## ⌚ Stochastic representation of the random assets

The equation of dynamic evolution of the random assets yields the representation

$$A(t) = (A(0)+P(0)) \cdot \exp\{Z(1,t)\} + \sum_{(k=1,\dots,t-1)} (P(k) - X(k)) \cdot \exp\{Z(k+1,t)\} - X(t)$$

$$Z(k,t) = \sum_{(j=k,\dots,t)} \ln\{R(j)\}, \quad t=1,\dots,T, \quad k=1,\dots,t$$

## ⌚ Market risk model assumptions

- (M1) *Full diversification* of the insurance *liability risk*:  $X(t) = r \cdot \pi(t-1)$ ,  $t=1,\dots,T$
- (M2) *Loaded* and *pure premium* processes  $P(t)$  and  $\pi(t)$  are *deterministic*
- (M3) *Log-returns*  $\ln\{R(t)\} \sim N(\mu, \sigma^2)$  are *independent* and *identically normally distributed*  
(Black-Scholes-Merton return model)

# Market Risk (2) mean and variance of random assets

## Mean and variance of the prospective random assets

- market risk model (M1)-(M3)
- $r_M = \exp\{\mu + \frac{1}{2}\sigma^2\}$  : *expected accumulated rate of return* over  $(t-1, t]$ ,  $t=1, \dots, T$
- $PV(a, r) = \sum_{(k=0, \dots, T-1)} a(k)/r^k$  : *present value* of vector  $a=(a(0), \dots, a(T-1))$  w.r.t.  $r$
- $PV(a, r_a; b, r_b) = \sum_{(0 \leq s < t \leq T-1)} a(s)b(t)/(r_a^s \cdot r_b^t)$  : *bivariate present value* of  $a, b$  w.r.t.  $r_a, r_b$
- $\Theta=(\Theta(0), \dots, \Theta(T-1)), \mu_P=(0, P(1), \dots, P(T-1)), \mu_x=r \cdot (0, \pi(0), \dots, \pi(T-2)).$

Under *fair value assumption*  $r_M=r$ , one has

$$E[v^T \cdot A(T)] = A(0) + PV(\Theta, r) \quad \& \quad \text{Var}[v^T \cdot A(T)] = (A(0) + P(0))^2 \cdot (e^{T\sigma^2} - 1) + S(1) + S(2) + S(3)$$

$$S(1) = 2 \cdot (A(0) + P(0)) \cdot (e^{T\sigma^2} \cdot PV(\mu_P - \mu_x, r \cdot e^{\sigma^2}) - PV(\mu_P - \mu_x, r))$$

$$S(2) = e^{T\sigma^2} \cdot PV((\mu_P - \mu_x)^2, r^2 \cdot e^{\sigma^2}) - PV((\mu_P - \mu_x)^2, r^2)$$

$$S(3) = 2 \cdot (e^{T\sigma^2} \cdot PV(\mu_P - \mu_x, r; \mu_P - \mu_x, r \cdot e^{\sigma^2}) - PV(\mu_P - \mu_x, r; \mu_P - \mu_x, r))$$

# Market Risk (3) Solvency II and SST economic capital

## ● Economic capital

$$EC = R[\Delta SC(1)] = C(0) - E[v \cdot C(1)] + R[LA(1)] \quad (R[\cdot] \text{ VaR or TVaR measure})$$

**LA(1)=E[v·A(1)]-v·A(1)** : 1<sup>st</sup> year *asset loss*

## ● 1<sup>st</sup> year Solvency II SCR (VaR measure)

$$VaR_\alpha[LA(1)] = \rho_{\alpha, VaR}(\sigma A(1)) \cdot (A(0) + \Theta(0)) \quad \text{with } \sigma A(1) \text{ coefficient of variation of } A(1)$$

$$\rho_{\alpha, VaR}(x) = 1 - \exp\{\Phi^{-1}(1-\alpha) \cdot \ln(1+x^2)^{1/2}\} / (1+x^2)^{1/2}$$

(up to sign change identical to non-life SCR VaR: **Hürlimann(2010a), (3.4)**)

## ● SST market risk EC (TVaR measure)

$$TVaR_\alpha[LA(1)] = \rho_{\alpha, TVaR}(\sigma A(1)) \cdot (A(0) + \Theta(0))$$

$$\rho_{\alpha, TVaR}(x) = 1 - \Phi\{\Phi^{-1}(1-\alpha) - \ln(1+x^2)^{1/2}\} / (1-\alpha)$$

(up to sign change identical to non-life SCR TVaR: **Hürlimann(2009b), (13.9)**)

# Market Risk (4) Solvency II versus SST economic capital

## Comparison of solvency capital ratios $\rho_{\alpha, \cdot}(\sigma A(1))/\sigma A(1)$

	VaR Method			CVaR Method		
confidence level	0.99	<b>0.995</b>	0.99612	<b>0.98720</b>	0.99	0.995
percentile	-2.326	<b>-2.576</b>	-2.662	<b>-2.232</b>	-2.326	-2.576
return volatility $\sigma$						
5.0%	2.216	<b>2.436</b>	2.512	<b>2.438</b>	2.512	2.709
5.5%	2.205	<b>2.422</b>	2.497	<b>2.424</b>	2.497	2.691
6.0%	2.194	<b>2.409</b>	2.482	<b>2.410</b>	2.482	2.674
6.5%	2.183	<b>2.395</b>	2.468	<b>2.396</b>	2.467	2.656
7.0%	2.172	<b>2.381</b>	2.453	<b>2.382</b>	2.453	2.639
<b>7.5%</b>	<b>2.162</b>	<b>2.368</b>	2.438	<b>2.368</b>	2.438	2.621
8.0%	2.151	<b>2.354</b>	2.424	<b>2.355</b>	2.423	2.604
8.5%	2.140	<b>2.341</b>	2.410	<b>2.341</b>	2.409	2.587
9.0%	2.129	<b>2.328</b>	2.395	<b>2.328</b>	2.394	2.570
9.5%	2.118	<b>2.314</b>	2.381	<b>2.314</b>	2.380	2.553
10.0%	2.108	<b>2.301</b>	2.367	<b>2.301</b>	2.365	2.536

# Market Risk (5) Solvency II and SST risk margin

## ● Risk margin (RM)

$RM = i_{CoC} \cdot (R[\Delta SC(2)] + R[\Delta SC(3)] + \dots + R[\Delta SC(T)])$  ( $R[\cdot]$  VaR or TVaR measure)

$R[\Delta SC(t)] = E[v^t \cdot (r \cdot C(t-1) - C(t))] + R[LA(t)], \quad t=2, \dots, T$

$LA(t) = E[v^t \cdot (A(t) - r \cdot A(t-1))] - v^t \cdot (A(t) - r \cdot A(t-1))$  :  $t^{\text{th}}$  year *asset loss*

## ● Solvency II RM (VaR measure)

$VaR_\alpha[LA(t)] = \rho_{\alpha, VaR}(\sigma A(t)) \cdot E[A(t) - r \cdot A(t-1)]$

$\sigma A(t)$  *coefficient of variation* of  $A(t) - r \cdot A(t-1)$

## ● SST RM (TVaR measure)

$TVaR_\alpha[LA(t)] = \rho_{\alpha, TVaR}(\sigma A(t)) \cdot E[A(t) - r \cdot A(t-1)]$

# Market Risk (6) coherent SST risk measure/target capital

## ● SST target capital via SST risk measure

$$TC_{\alpha,SST} = C(0) + R_{\alpha,SST}[SC] \quad \text{with}$$

$$R_{\alpha,SST}[SC] = TVaR_{\alpha}[SC(1)] + i_{CoC} \cdot \sum_{(t=2, \dots, T)} TVaR_{\alpha}[\Delta SC(t)] \quad \text{SST risk measure}$$

*not a coherent* multi-period risk measure (**Filipovic and Vogelpoth(2008)**):

$$X \geq Y \Rightarrow R_{\alpha,SST}[X] \geq R_{\alpha,SST}[Y] \quad \text{does not always hold!}$$

## ● Coherent SST target capital via coherent SST risk measure

$$TC_{\alpha,SST,c} = C(0) + R_{\alpha,SST,c}[SC] \quad \text{with}$$

$$R_{\alpha,SST,c}[SC] = (1 - i_{CoC}) \cdot TVaR_{\alpha}[SC(1)] + i_{CoC} \cdot TVaR_{\alpha}[SC(T)] \quad \text{coherent SST measure}$$

$$TC_{\alpha,SST,c} = C(0) - E[v \cdot C(1)] + i_{CoC} \cdot E[v \cdot C(1) - v^t \cdot C(T)] + R^*_{\alpha,SST,c}[A(1), A(T)] \quad \text{with}$$

$$R^*_{\alpha,SST,c}[A(1), A(T)]$$

$$= (1 - i_{CoC}) \cdot \rho_{\alpha, TVaR}(\sigma A(1)) \cdot (A(0) + \Theta(0)) + i_{CoC} \cdot \rho_{\alpha, TVaR}(\sigma A(T)) \cdot (A(0) + PV(\Theta, r))$$

and  $\sigma A(1)$ ,  $\sigma A(T)$  the *coefficients of variation* of  $A(1)$ ,  $A(T)$

# Market Risk (7) coherent SST target capital life insurance

## ⌚ Portfolio of identical life insurance policies

- $\pi(0)=\pi$  : pure level premium
- $\theta(t)=\theta$  : constant premium loading factor,  $t=0, \dots, T-1$
- $\pi(t-1)=t-1 p_x \cdot \pi$  : pure premium at time  $t-1$ ,  $t=1, \dots, T$ , with
- $t-1 p_x$  : survival probability of a life aged  $x$  at initial time  $t=0$

## ⌚ Analytical evaluation of coherent SST target capital

Our evaluation of *coherent SST market risk ratios*  $R^*_{\alpha, SST, c} [SC] / A(0)$  uses the formulas

$$\sigma A(1)^2 = (1 + \pi / (A(0) + \theta \cdot \pi))^2 \cdot (e^{\sigma^2} - 1)$$

$$\sigma A(T)^2 = ((A(0) + (1 + \theta) \cdot \pi)^2 \cdot (e^{T\sigma^2} - 1) + S(1) + S(2) + S(3)) / (A(0) + PV(\theta, r))^2$$

$$\sigma A^*(T)^2 = ((A(0) + (1 + \theta) \cdot \pi) / (A(0) + PV(\theta, r))^2 \cdot (e^{T\sigma^2} - 1) \quad \text{simple approximation}$$

and the parameter values

$\alpha=99\%$ ,  $\sigma=7.5\%$ ,  $\pi=100$ ,  $\theta=10\%$ ,  $A(0)=1000$ ,  $r=1.025$ ,  $i_{CoC}=6\%$

# Market Risk (8) coherent SST market risk ratios / $\sigma=7.5\%$

$\alpha$	0.99	coherent SST risk measure ratio by varying time horizon														
T	T-1px	$a=\mu_p - \mu_x$	PV( $\theta, v$ )	PV( $a, v$ )	PV( $a, v\sigma$ )	S1	S2	S3	$\sigma_{A1}$	$\sigma_{AT}$	$\sigma_{A^*T}$	$\rho_{\alpha}(\sigma_{A1})$	$\rho_{\alpha}(\sigma_{AT})$	$\rho_{\alpha}(\sigma_{A^*T})$	Rc/Ao	R*c/Ao
1	1.00000	7.402	10.0	0.0	0.0	0	0.0	0.0	8.3%	8.3%	8.3%	20.0%	20.0%	20.0%	20.0%	20.0%
2	0.99911	7.387	19.7	7.2	7.2	90	0.3	0.0	8.3%	11.6%	11.6%	20.0%	27.0%	26.9%	20.4%	20.4%
3	0.99815	7.371	29.2	14.3	14.1	269	0.9	0.6	8.3%	14.2%	14.1%	20.0%	31.9%	31.8%	20.7%	20.7%
4	0.99710	7.353	38.5	21.1	20.9	535	1.7	1.7	8.3%	16.3%	16.1%	20.0%	35.8%	35.5%	21.0%	21.0%
5	0.99596	7.334	47.5	27.8	27.4	886	2.8	3.3	8.3%	18.1%	17.9%	20.0%	39.0%	38.6%	21.2%	21.2%
6	0.99473	7.313	56.3	34.2	33.7	1320	4.1	5.5	8.3%	19.8%	19.5%	20.0%	41.7%	41.2%	21.4%	21.4%
7	0.99338	7.290	64.9	40.5	39.8	1835	5.7	8.1	8.3%	21.3%	20.9%	20.0%	44.1%	43.5%	21.6%	21.5%
8	0.99193	7.266	73.2	46.7	45.7	2430	7.5	11.1	8.3%	22.7%	22.2%	20.0%	46.2%	45.5%	21.7%	21.7%
9	0.99035	7.239	81.4	52.6	51.4	3103	9.5	14.6	8.3%	24.0%	23.4%	20.0%	48.1%	47.2%	21.9%	21.8%
10	0.98863	7.210	89.3	58.4	56.9	3852	11.7	18.5	8.3%	25.2%	24.5%	20.0%	49.8%	48.8%	22.0%	22.0%
11	0.98677	7.179	97.0	64.1	62.2	4676	14.1	22.8	8.3%	26.3%	25.6%	20.0%	51.3%	50.3%	22.1%	22.1%
12	0.98475	7.145	104.5	69.5	67.4	5573	16.7	27.5	8.3%	27.4%	26.6%	20.0%	52.8%	51.6%	22.3%	22.2%
13	0.98256	7.108	111.8	74.9	72.3	6542	19.5	32.5	8.3%	28.5%	27.5%	20.0%	54.1%	52.9%	22.4%	22.3%
14	0.98019	7.068	118.9	80.0	77.1	7581	22.4	37.8	8.3%	29.5%	28.4%	20.0%	55.4%	54.0%	22.5%	22.4%
15	0.97761	7.025	125.8	85.0	81.7	8688	25.4	43.5	8.3%	30.4%	29.3%	20.0%	56.5%	55.1%	22.6%	22.5%
16	0.97482	6.978	132.6	89.9	86.2	9863	28.7	49.5	8.3%	31.3%	30.1%	20.0%	57.6%	56.1%	22.7%	22.6%
17	0.97179	6.928	139.1	94.6	90.5	11103	32.0	55.8	8.3%	32.2%	30.9%	20.0%	58.6%	57.1%	22.8%	22.7%
18	0.96851	6.873	145.5	99.1	94.6	12406	35.5	62.3	8.3%	33.1%	31.6%	20.0%	59.6%	58.0%	22.9%	22.8%
19	0.96496	6.814	151.7	103.5	98.6	13773	39.2	69.1	8.3%	33.9%	32.4%	20.0%	60.5%	58.8%	23.0%	22.8%
20	0.96111	6.750	157.7	107.8	102.4	15200	42.9	76.2	8.3%	34.8%	33.1%	20.0%	61.4%	59.6%	23.0%	22.9%

# Market Risk (9) coherent SST market risk ratios / $\sigma=5\%$

$\alpha$	0.99	coherent SST risk measure ratio by varying time horizon														
T	T-1px	$a=\mu_p - \mu_x$	PV( $\theta, v$ )	PV( $a, v$ )	PV( $a, v_0$ )	S1	S2	S3	$\sigma_{A1}$	$\sigma_{At}$	$\sigma_{A^*T}$	$\rho_\alpha(\sigma_{A1})$	$\rho_\alpha(\sigma_{At})$	$\rho_\alpha(\sigma_{A^*T})$	$Rc/A_0$	$R^*_c/A_0$
1	1.00000	7.402	10.0	0.0	0.0	0	0.0	0.0	5.5%	5.5%	5.5%	13.7%	13.7%	13.7%	13.7%	13.7%
2	0.99911	7.387	19.7	7.2	7.2	40	0.1	0.0	5.5%	7.7%	7.7%	13.7%	18.8%	18.8%	14.1%	14.1%
3	0.99815	7.371	29.2	14.3	14.2	119	0.4	0.3	5.5%	9.4%	9.4%	13.7%	22.5%	22.3%	14.3%	14.3%
4	0.99710	7.353	38.5	21.1	21.0	237	0.8	0.7	5.5%	10.8%	10.7%	13.7%	25.4%	25.2%	14.5%	14.5%
5	0.99596	7.334	47.5	27.8	27.6	392	1.2	1.5	5.5%	12.0%	11.9%	13.7%	27.8%	27.5%	14.7%	14.6%
6	0.99473	7.313	56.3	34.2	34.0	583	1.8	2.4	5.5%	13.1%	12.9%	13.7%	29.9%	29.6%	14.8%	14.8%
7	0.99338	7.290	64.9	40.5	40.2	810	2.5	3.6	5.5%	14.1%	13.8%	13.7%	31.8%	31.3%	14.9%	14.9%
8	0.99193	7.266	73.2	46.7	46.2	1071	3.3	4.9	5.5%	15.0%	14.7%	13.7%	33.5%	32.9%	15.1%	15.0%
9	0.99035	7.239	81.4	52.6	52.1	1366	4.2	6.4	5.5%	15.9%	15.5%	13.7%	35.0%	34.4%	15.2%	15.1%
10	0.98863	7.210	89.3	58.4	57.7	1695	5.2	8.2	5.5%	16.7%	16.2%	13.7%	36.4%	35.7%	15.3%	15.2%
11	0.98677	7.179	97.0	64.1	63.2	2055	6.2	10.0	5.5%	17.4%	16.9%	13.7%	37.7%	36.9%	15.4%	15.3%
12	0.98475	7.145	104.5	69.5	68.6	2447	7.3	12.1	5.5%	18.1%	17.5%	13.7%	38.9%	38.0%	15.5%	15.4%
13	0.98256	7.108	111.8	74.9	73.7	2869	8.5	14.3	5.5%	18.8%	18.1%	13.7%	40.1%	39.0%	15.6%	15.5%
14	0.98019	7.068	118.9	80.0	78.7	3320	9.8	16.6	5.5%	19.4%	18.7%	13.7%	41.1%	40.0%	15.7%	15.6%
15	0.97761	7.025	125.8	85.0	83.5	3801	11.1	19.1	5.5%	20.0%	19.3%	13.7%	42.1%	40.9%	15.8%	15.7%
16	0.97482	6.978	132.6	89.9	88.2	4310	12.5	21.6	5.5%	20.6%	19.8%	13.7%	43.1%	41.7%	15.8%	15.8%
17	0.97179	6.928	139.1	94.6	92.7	4846	14.0	24.4	5.5%	21.2%	20.3%	13.7%	44.0%	42.5%	15.9%	15.8%
18	0.96851	6.873	145.5	99.1	97.1	5409	15.5	27.2	5.5%	21.8%	20.8%	13.7%	44.8%	43.3%	16.0%	15.9%
19	0.96496	6.814	151.7	103.5	101.3	5998	17.0	30.1	5.5%	22.3%	21.3%	13.7%	45.6%	44.0%	16.1%	16.0%
20	0.96111	6.750	157.7	107.8	105.4	6612	18.7	33.2	5.5%	22.8%	21.7%	13.7%	46.4%	44.7%	16.1%	16.0%

# References (1)

- Doff, R. (2007). Risk Management for Insurers – Risk Control, Economic Capital and Solvency II. Risk Books, Incisive Media, London.
- Filipovic , D. and N. Vogelpoth (2008). A note on the Swiss Solvency Test risk measure. Insurance: Mathematics and Economics 42, 897-902.
- FOPI (2004). White Paper of the Swiss Solvency Test.  
[http://www.finma.ch/archiv/bpv/download/e/WhitePaperSST\\_en.pdf](http://www.finma.ch/archiv/bpv/download/e/WhitePaperSST_en.pdf)
- FOPI (2006). Technical document on the Swiss Solvency Test.  
[http://www.finma.ch/archiv/bpv/download/e/SST\\_techDok\\_061002\\_E\\_wo\\_Li\\_20070118.pdf](http://www.finma.ch/archiv/bpv/download/e/SST_techDok_061002_E_wo_Li_20070118.pdf)
- Gisler, A. (2009). The insurance risk in the SST and in Solvency II: modeling and parameter estimation. 39<sup>th</sup> International ASTIN Colloquium, Helsinki.
- Hürlimann, W. (2001). Analytical evaluation of economic risk capital for portfolios of Gamma risks. ASTIN Bulletin 31, 107-122.
- Hürlimann, W. (2002). Analytical bounds for two value-at-risk functionals. ASTIN Bulletin 32(2), 235-265.
- Hürlimann, W. (2003). Conditional value-at-risk bounds for compound Poisson risks and a normal approximation. Journal of Applied Mathematics 3(3), 141-154.

## References (2)

- Hürlimann, W. (2009a). On the optimal SST initial capital of a life contract. In: M. Cruz (Editor). *The Solvency II Handbook*, Chapter 17. Risk books, Incisive Media, London.
- Hürlimann, W. (2009b). On the non-life Solvency II model. In: M. Cruz (Editor). *The Solvency II Handbook*, Chapter 17. Risk books, Incisive Media, London.
- Hürlimann, W. (2010a). Modelling non-life insurance risk for Solvency II in a reinsurance context. *Life & Pensions Magazine*, January 2010, 35-40.
- Hürlimann, W. (2010b). Solvency II life insurance risk for portfolios of general life contracts. *Mathematical and Statistical Methods for Actuarial Science and Finance*, Villa Rufolo – Ravello, Italy, 7-9 April 2010. <http://maf2010.unisa.it/>
- Kaufmann, R. and A. Wyler (2005). Summary on the Swiss Solvency Test. *De Actuaris*, Bulletin van het Actuarieel Genootschap 12(4), 43-45.
- QIS4 (2008). Technical Specifications QIS4 – CEIOPS Quantitative Impact Study 4, March 31, 2008. Available at <http://www.ceiops.org>.

# Discussion

## Q&A

# Thank You

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